Understanding Cryptography – A Textbook for Students and Practitioners

by Christof Paar and Jan Pelzl

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Chapter 11 – Hash Functions

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These slides were prepared by Stefan Heyse and Christof Paar and Jan Pelzl

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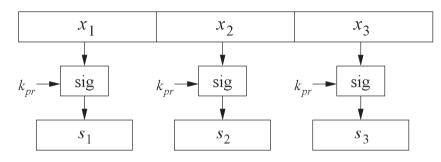
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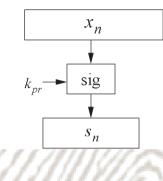
- Why we need hash functions
- How does it work
- Security properties
- Algorithms
- Example: The Secure Hash Algorithm SHA-1

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Naive signing of long messages generates a signature of same length.





- Three Problems
- Computational overhead
- Message overhead
- Security limitations
- For more info see Section 11.1 in "Understanding Cryptography".

Solution:

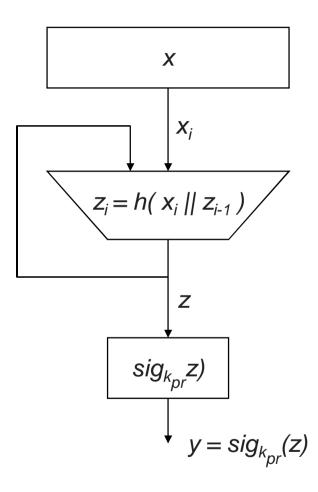
Instead of signing the whole message, sign only a digest (=hash)

Also secure, but much faster

Needed:

Hash Functions Chapter 11 of Understanding Cryptography by Christof Paar and Jan Pelzl

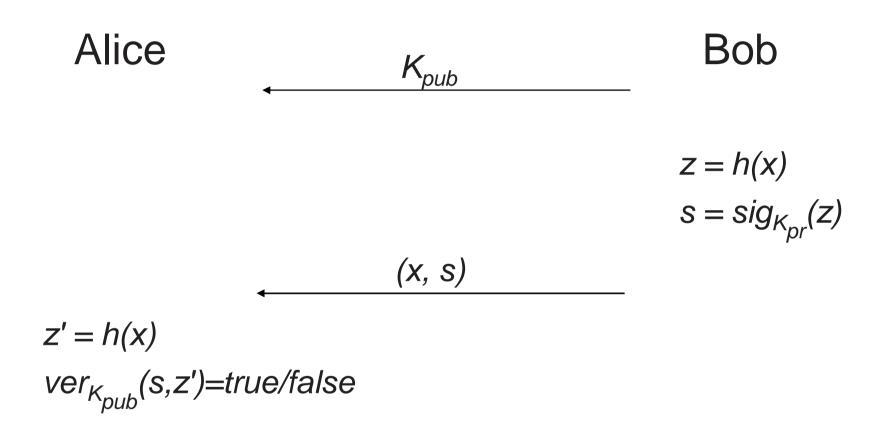
Digital Signature with a Hash Function



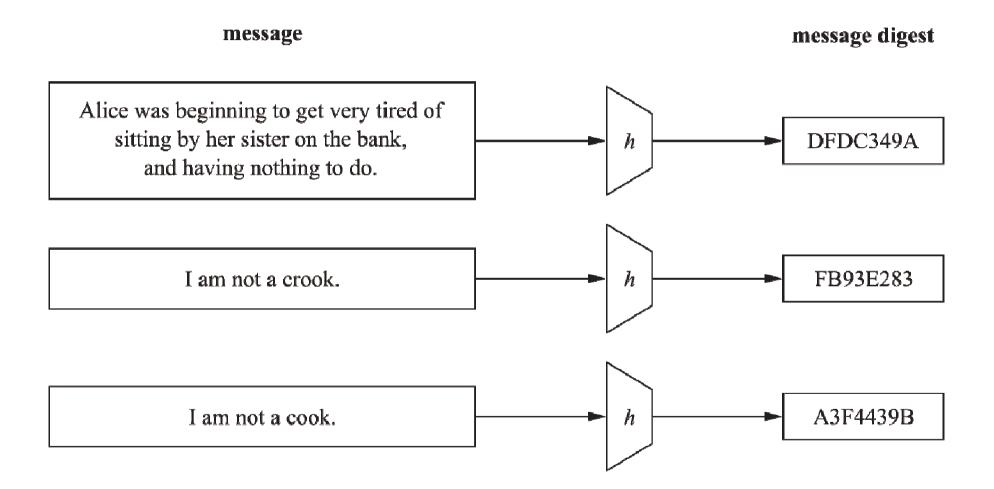
Notes:

- x has fixed length
- *z, y* have fixed length
- *z*, *x* do not have equal length in general
- h(x) does not require a key.
- h(x) is public.

Basic Protocol for Digital Signatures with a Hash Function:

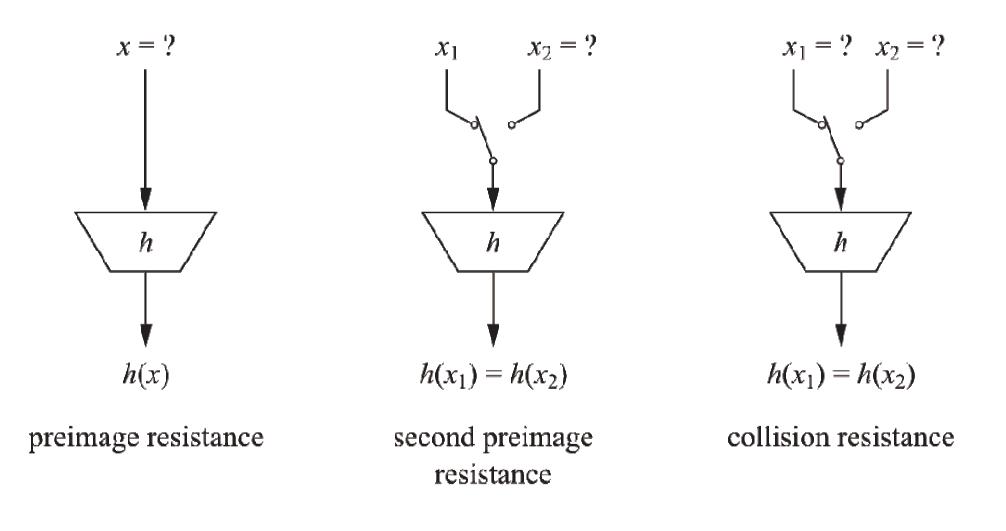


Principal input–output behavior of hash functions



- Why we need hash functions
- How does it work
- Security properties
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The three security properties of hash functions



Hash Funktionen: Security Properties

- Preimage resistance: For a given output z, it is impossible to find any input x such that h(x) = z, i.e., h(x) is one-way.
- Second preimage resistance: Given x_1 , and thus $h(x_1)$, it is computationally infeasible to find any x_2 such that $h(x_1) = h(x_2)$.
- Collision resistance: It is computationally infeasible to find any pairs $x_1 \neq x_2$ such that $h(x_1) = h(x_2)$.

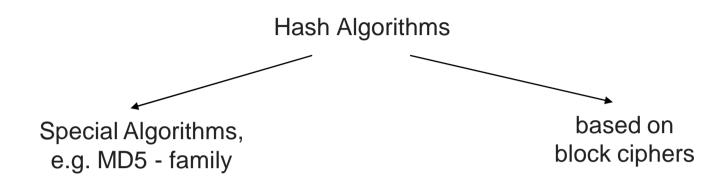
Hash Funktionen: Security

It turns out that collison resistance causes most problems

- How hard is it to find a collision with a probability of 0.5 ?
- Related Problem: How many people are needed such that two of them have the same birthday with a probability of 0.5 ?
- No! Not 365/2=183. 23 are enough ! This is called the birthday paradoxon (Search takes ≈√2ⁿ steps).
- For more info see Chapter 11.2.3 in Understanding Cryptography.
- To deal with this paradox, hash functions need a output size of at least 160 bits.

- Why we need hash functions
- How does it work
- Security properties
- Algorithms
- Example: The Secure Hash Algorithm SHA-1





- MD5 family
- SHA-1: output 160 Bit; input 512 bit chunks of message x; operations - bitwise AND, OR, XOR, complement und cyclic shifts.
- RIPE-MD 160: output 160 Bit; input 512 bit chunks of message x; operations – like in SHA-1, but two in parallel and combinations of them after each round.

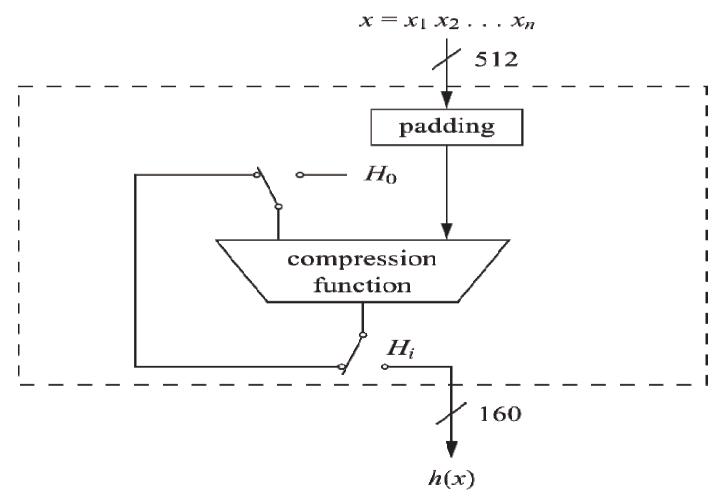
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SHA-1

- Part of the MD-4 family.
- Based on a Merkle-Dåmgard construction.
- 160-bit output from a message of maximum length 2⁶⁴ bit.
- Widely used (even tough some weaknesses are known)

SHA-1 High Level Diagramm

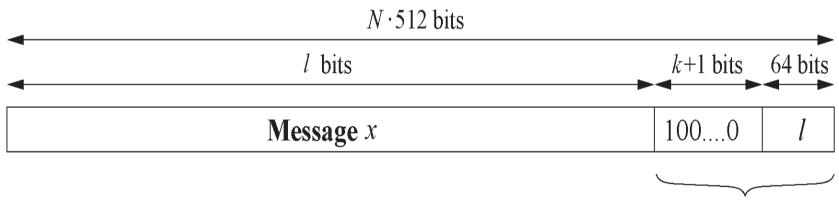
• Compression Function consists of 80 rounds which are divided into four stages of 20 rounds each



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SHA-1: Padding

- Message x has to be padded to fit a size of a multiple of 512 bit.
- $k \equiv 512 64 1 1 = 448 (1 + 1) \mod 512$.



Padding

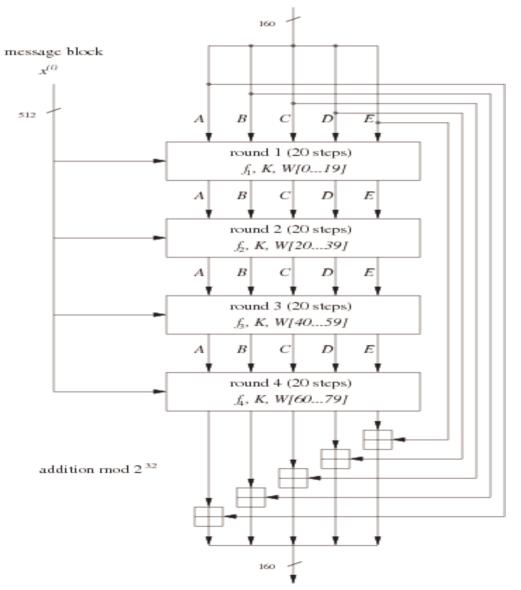
SHA-1: Hash Computation

• Each message block x_i is processed in four stages with 20 rounds each

SHA-1 uses:

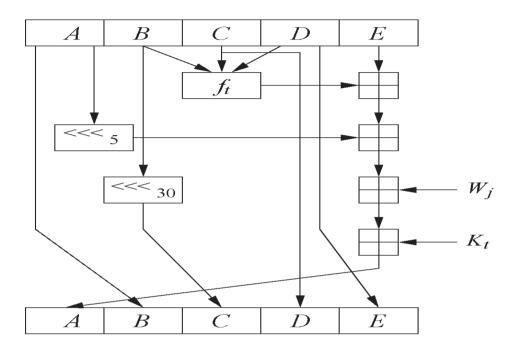
- A message schedule which computes a 32-bit word W0,W1,...,W79 for each of the 80 rounds
- Five working registers of size of 32 bits A,B,C,D,E
- A hash value H_i consisting of five 32-bit words $H_i^{(0)}$, $H_i^{(1)}$, $H_i^{(2)}$, $H_i^{(3)}$, $H_i^{(4)}$
- In the beginning, the hash value holds the initial value H₀, which is replaced by a new hash value after the processing of each single message block.
- The final hash value H_n is equal to the output h(x) of SHA-1.

SHA-1: All four stages



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SHA-1: Internals of a Round



Stage t	Round j	Constant K _t	Function f _t
1	0019	K=5A827999	$f(B,C,D)=(B\land C)\lor(^{-}B\land D)$
2	2039	K=6ED9EBA1	$f(B,C,D)=B\oplus C\oplus D$
3	4059	K=8F1BBCDC	$f(B,C,D)=(B\oplus C)\vee(B\oplus D)\vee(C\oplus D)$
4	6079	K=CA62C1D6	$f(B,C,D)=B\oplus C\oplus D$

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Lessons Learned: Hash-Funktionen

- Hash functions are keyless. The two most important applications of hash functions are their use in digital signatures and in message authentication codes such as HMAC.
- The three security requirements for hash functions are one-wayness, second preimage resistance and collision resistance.
- Hash functions should have at least 160-bit output length in order to withstand collision attacks; 256 bit or more is desirable for long-term security.
- MD5, which was widely used, is insecure. Serious security weaknesses have been found in SHA-1, and the hash function should be phased out. The SHA-2 algorithms all appear to be secure.
- The ongoing SHA-3 competition will result in new standardized hash functions in a few years.